

Lesson 23: Solution Sets to Simultaneous Equations

Classwork

Opening Exercise

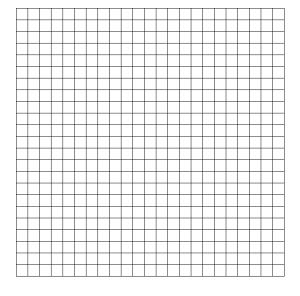
Here is a system of two linear equations. Verify that the solution to this system is (3,4).

Equation A1: y = x + 1

Equation A2: y = -2x + 10

Exploratory Challenge

- a. Write down another system of two linear equations, B1 and B2, whose solution is (3, 4). This time make sure both linear equations have a positive slope.
- b. Verify that the solution to this system of two linear equations is (3,4).
- c. Graph equation B1 and B2.
- d. Are either B1 or B2 equivalent to the original A1 or A2? Explain your reasoning.





3: Solution Sets to Simultaneous Equations







e. Add A1 and A2 to create a new equation C1. Then, multiply A1 by 3 to create a new equation C2. Why is the solution to this system also (3, 4)? Explain your reasoning.

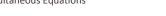
The following system of equations was obtained from the original system by adding a multiple of equation A2 to equation A1.

Equation D1: y = x + 1Equation D2: 3y = -3x + 21

- f. What multiple of A2 was added to A1 to create D2?
- g. What is the solution to the system of two linear equations formed by D1 and D2?
- h. Is D2 equivalent to the original A1 or A2? Explain your reasoning.
- i. Start with equation A1. Multiply it by a number of your choice and add the result to equation A2. This creates a new equation E2. Record E2 below to check if the solution is (3,4).

Equation E1: y = x + 1Equation E2:







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Example: Why Does the Elimination Method Work?

Solve this system of linear equations algebraically.

ORIGINAL SYSTEM $2x + y = 6$	NEW SYSTEM	SOLUTION
x - 3y = -11		

Exercises

Explain a way to create a new system of equations with the same solution as the original that eliminates variable y 1. from one equation. Then determine the solution.

ORIGINAL SYSTEM	NEW SYSTEM	SOLUTION
2x + 3y = 7		
x - y = 1		

2. Explain a way to create a new system of equations with the same solution as the original that eliminates variable x from one equation. Then determine the solution.

ORIGINAL SYSTEM	NEW SYSTEM	SOLUTION
2x + 3y = 7		
x - y = 1		

Solution Sets to Simultaneous Equations



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Problem Set

Try to answer the following without solving for x and y first:

- 1. If 3x + 2y = 6 and x + y = 4, then
 - a. 2x + y = ? b. 4x + 3y = ?
- 2. You always get the same solution no matter which two of the four equations you choose from Problem 1 to form a system of two linear equations. Explain why this is true.
- 3. Solve the system of equations $\begin{cases} y = \frac{1}{4}x \\ y = -x + 5 \end{cases}$ by graphing. Then, create a new system of equations that has the same solution. Show either algebraically or graphically that the systems have the same solution.
- 4. Without solving the systems, explain why the following systems must have the same solution.

System (i):	4x - 5y = 13	System (ii):	8x - 10y = 26
	3x + 6y = 11		x - 11y = 2

Solve each system of equations by writing a new system that eliminates one of the variables.

- 5. 2x + y = 254x + 3y = 9
- $\begin{array}{ll} 6. & 3x + 2y = 4\\ & 4x + 7y = 1 \end{array}$





